

CERTAIN TRANSFORMATIONS INVOLVING POLY-BASIC
HYPERGEOMETRIC SERIES

Swatantra Kumar Shukla

Department of Mathematics,
Handia PG College, Prayagraj-221503, UP, INDIA

E-mail : swatantraplp1973@gmail.com

(Received: Jul. 25, 2019 Accepted: Dec. 10, 2019 Published: Apr. 30, 2020)

Abstract: In this paper, making use of Bailey transform and certain known summation formulas an attempt has been made to establish transformation formulas for poly-basic hypergeometric series.

Keywords and Phrases: Summation formula, transformation formula, Bailey transform, poly-basic hypergeometric series.

2010 Mathematics Subject Classification: Primary 33D15, 33D90, 11A55; Secondary 11F20, 33F05.

1. Introduction, Notations and Definitions

For real or complex q ($|q| < 1$), the q -shifted factorial is defined by,

$$[\alpha; q]_n = \begin{cases} 1, & \text{if } n = 0 \\ (1 - \alpha)(1 - \alpha q)(1 - \alpha q^2) \dots (1 - \alpha q^{n-1}), & \text{if } n = 1, 2, 3, \dots \end{cases} \quad (1.1)$$

Also,

$$[\alpha; q]_\infty = \prod_{n=0}^{\infty} (1 - \alpha q^n). \quad (1.2)$$

A basic hypergeometric function is defined as,

$${}_r\Phi_s \left[\begin{matrix} a_1, a_2, \dots, a_r; q; z \\ b_1, b_2, \dots, b_s; q^\lambda \end{matrix} \right] = \sum_{n=0}^{\infty} \frac{[a_1, a_2, \dots, a_r; q]_n z^n q^{\lambda n(n-1)/2}}{[q, b_1, b_2, \dots, b_s; q]_n}, \quad (1.3)$$